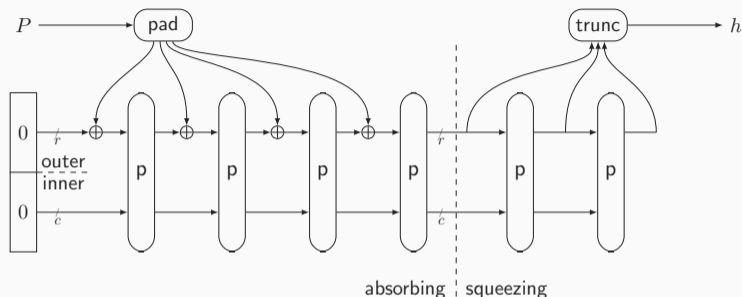


Understanding the Duplex and Its Security

Bart Mennink
Radboud University (The Netherlands)
Permutation-Based Crypto 2023, Lyon
April 23, 2023



History Sponges and Duplexes



- p is a b -bit permutation, with $b = r + c$
 - r is the rate
 - c is the capacity (security parameter)
- SHA-3, XOFs, lightweight hashing, ...
- Behaves as RO up to query complexity $\approx 2^{c/2}$ [BDPV08]

Keyed Sponge

- $\text{PRF}(K, P) = \text{sponge}(K \| P)$
- Message authentication with tag size t : $\text{MAC}(K, P, t) = \text{sponge}(K \| P, t)$
- Keystream generation of length ℓ : $\text{SC}(K, D, \ell) = \text{sponge}(K \| D, \ell)$
- (All assuming K is fixed-length)

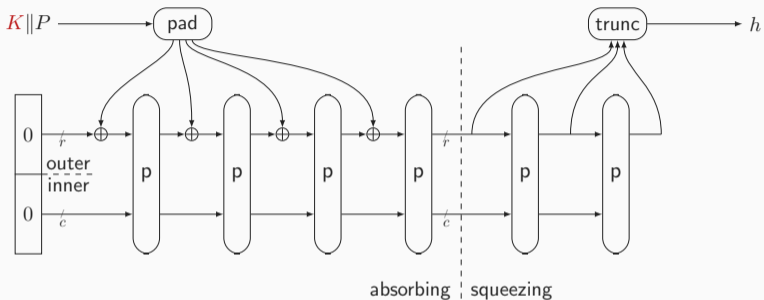
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Keyed Duplex

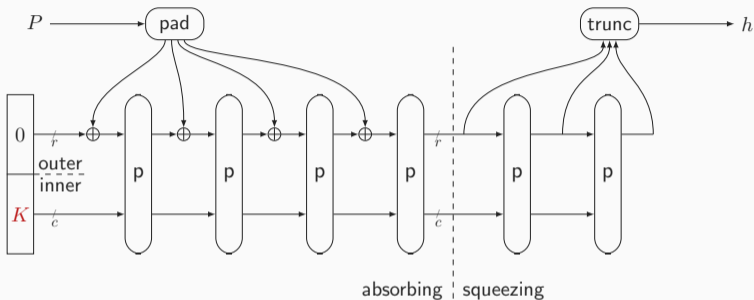
- Authenticated encryption
- Multiple CAESAR and NIST LWC submissions

Evolution of Keyed Sponges



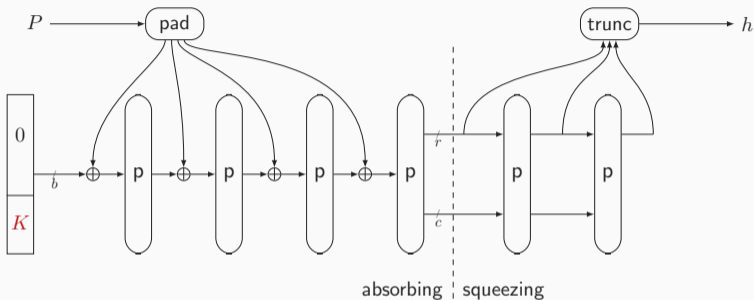
- Outer-Keyed Sponge [BDPV11b, ADMV15, NY16, Men18]

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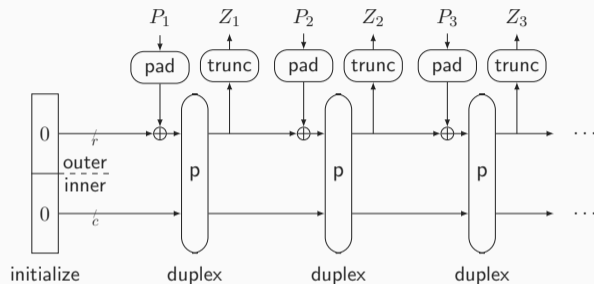
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Evolution of Keyed Sponges



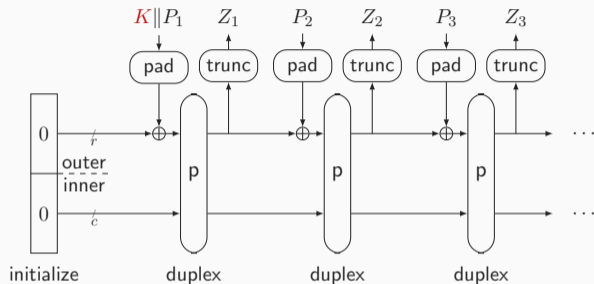
- Outer-Keyed Sponge [BDPV11b, ADMV15, NY16, Men18]
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Evolution of Keyed Duplexes



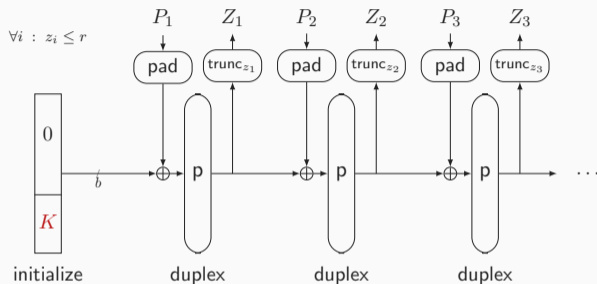
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Evolution of Keyed Duplexes



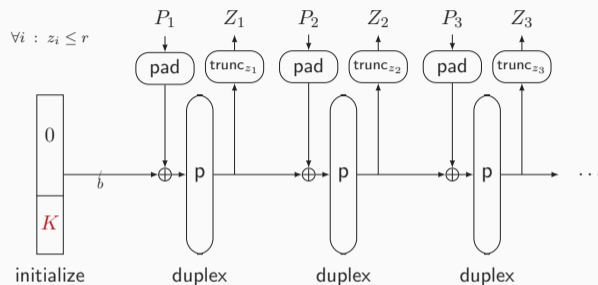
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Evolution of Keyed Duplexes



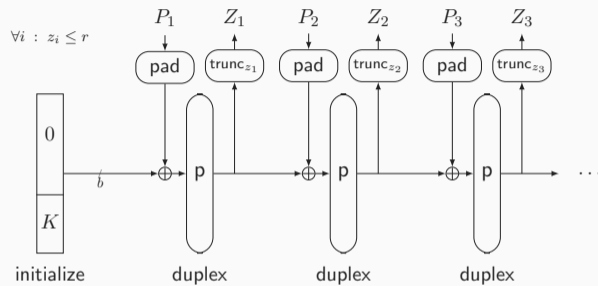
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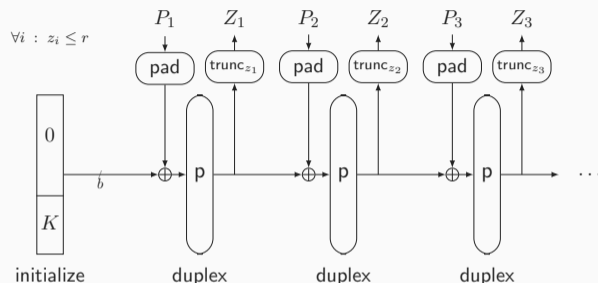


- Unkeyed Duplex [BDPV11a]
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Full-Keyed Duplex of [MRV15] (1)



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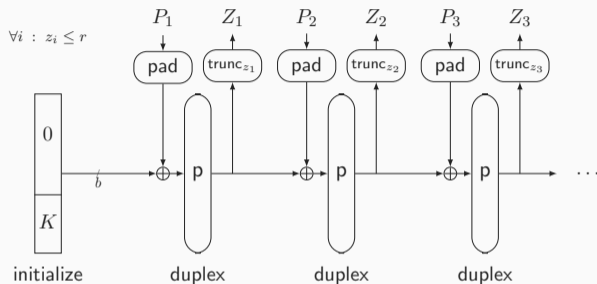


- M : data complexity (calls to construction)
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- $\mu \leq 2M$: multiplicity (“maximum outer collision of p ”)

Simplified Security Bound

$$\frac{\mu N}{2^k} + \frac{M^2}{2^c}$$

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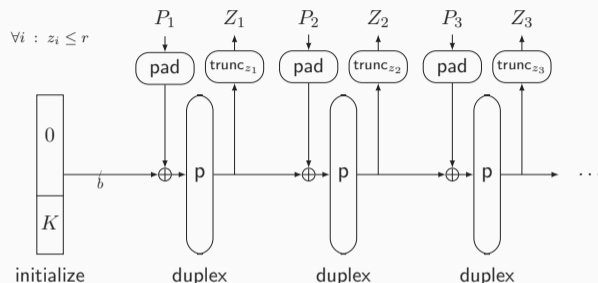
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scheme behaves “randomly” as long as this term is $\ll 1$

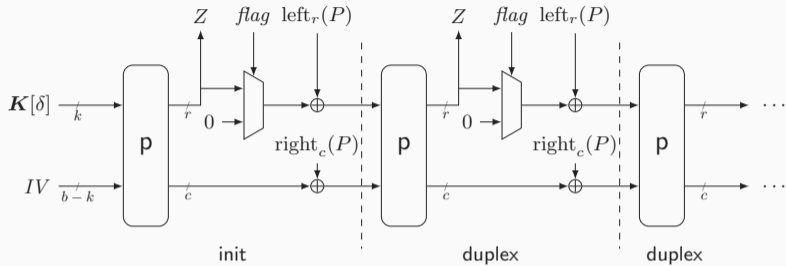
Full-Keyed Duplex of [MRV15] (2)



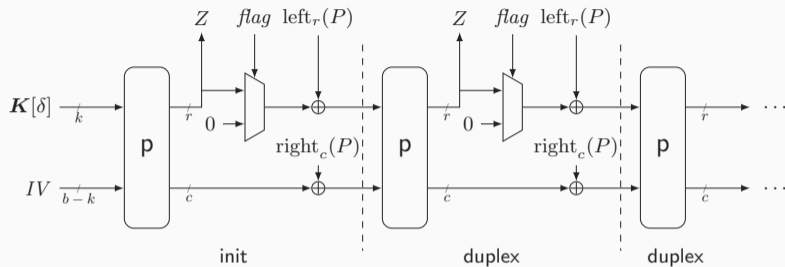
Limitations

- Multiplicity μ only known a posteriori
- Dominating term $\mu N/2^k$ rather than $\mu N/2^c$
- Limited flexibility in modeling adversarial power (multi-user security, blockwise adaptive behavior, nonces, ...)

Full-Keyed Duplex of [DMV17] (1)



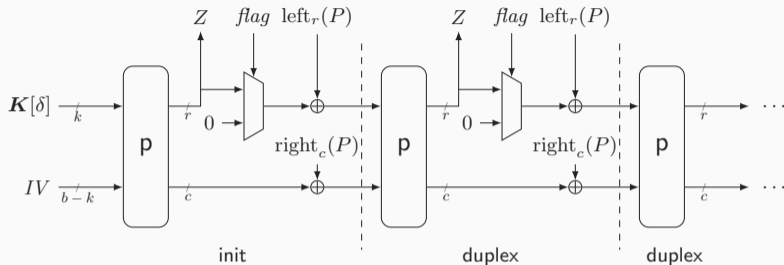
Full-Keyed Duplex of [DMV17] (1)



Features

- Multi-user by design: index δ specifies key in array
- Initial state: concatenation of $K[\delta]$ and IV
- Full-state absorption, no padding
- Rephasing: p, Z, P instead of P, p, Z
- Refined adversarial strength

Full-Keyed Duplex of [DMV17] (2)

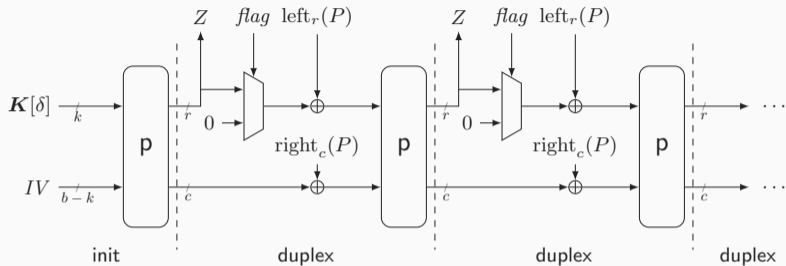


- M : data complexity (calls to construction)
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- Q : number of init calls
- Q_{IV} : max # init calls for single IV
- L : # queries with repeated path (e.g., nonce-violation)
- Ω : # queries with overwriting outer part (e.g., RUP)
- $\nu_{r,c}^M$: some multicollision coefficient (often small)

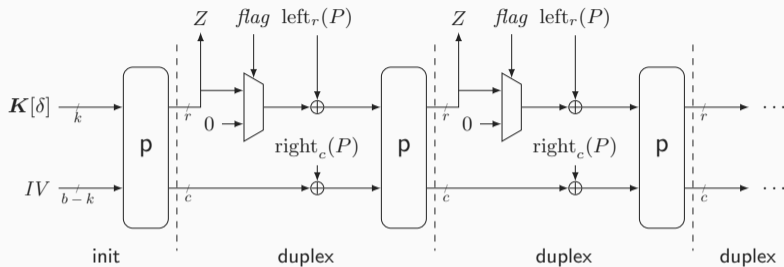
Simplified Security Bound

$$\frac{Q_{IV}N}{2^k} + \frac{(L + \Omega + \nu_{r,c}^M)N}{2^c}$$

Full-Keyed Duplex of [DM19] (1)



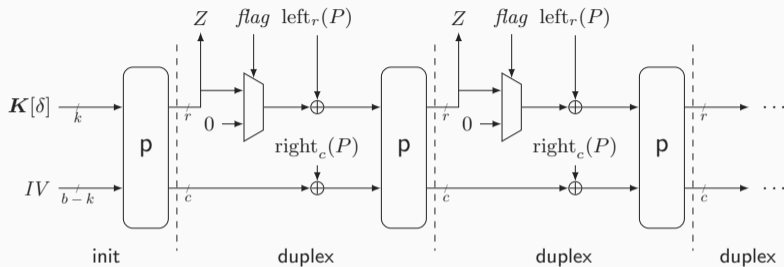
Full-Keyed Duplex of [DM19] (1)



Features

- Initialization can be rotated (not depicted)
- Another rephasing: Z, P, p instead of p, Z, P instead of P, p, Z
- Security analysis in leaky setting
- Even further refined adversarial strength
- Comparable bound

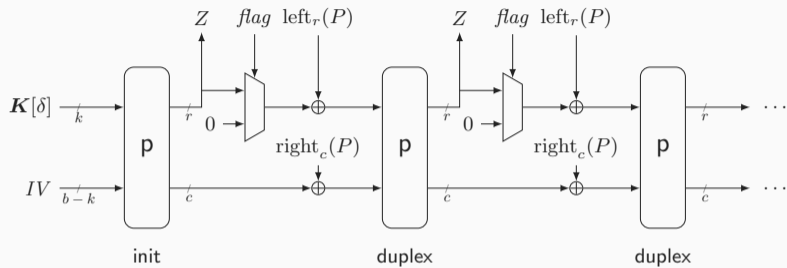
Full-Keyed Duplex of [DM19] (2)

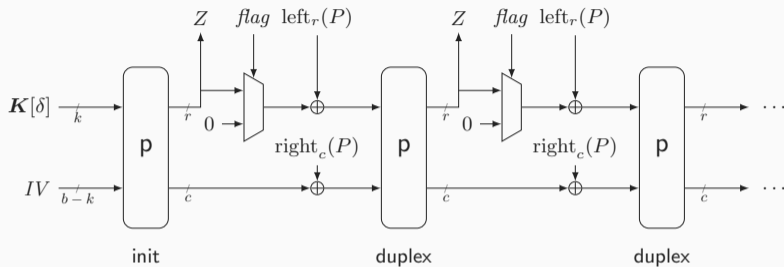


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- Q_{IV} : max # init calls for single IV
- Q_δ : maximum # init calls for single δ
- L : # queries with repeated path (e.g., nonce-violation)
- Ω : # queries with overwriting outer part (e.g., RUP)
- R : max # duplexing calls for single non-empty path
- $\nu_{r,c}^M$: some multicollision coefficient (often small)

Simplified Security Bound

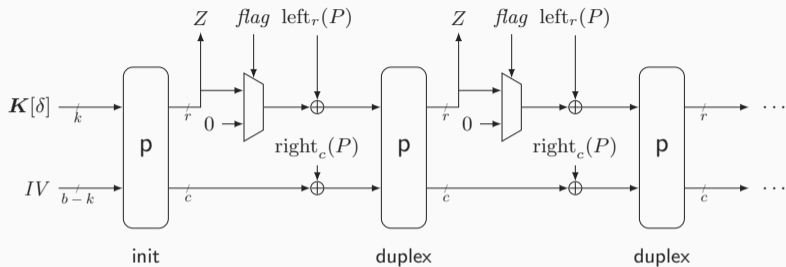
$$\frac{Q_{IV}N}{2^{k-Q_\delta\lambda}} + \frac{(L + \Omega + \nu_{r,c}^M)N}{2^{c-(R+1)\lambda}}$$





Scheme: versatile but complex

- What about these rephasings?
- What about the flag?

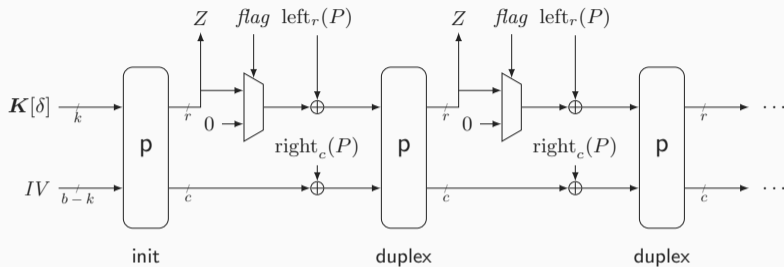


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Security bounds: strong but complex

- Security parameters hard to understand
- Bound quickly misunderstood
- Unclear how use case affects bound



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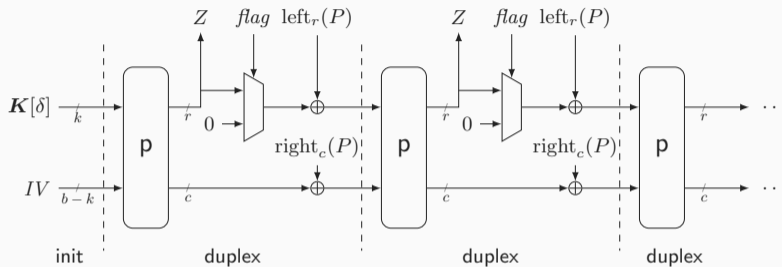
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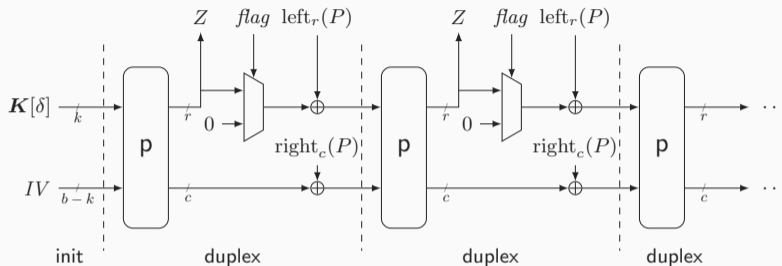
This work: explanation of the duplex, its security, and some applications

Understanding the Duplex

Generalized Keyed Duplex



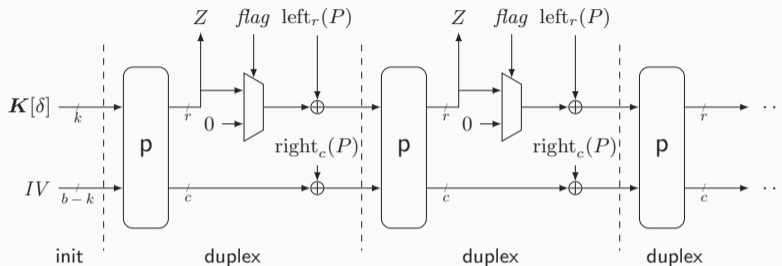
Generalized Keyed Duplex



Features

- Basically the scheme of [DMV17] and [DM19], but:
 - including possible initial state rotation (not depicted)
 - yet another rephrasing

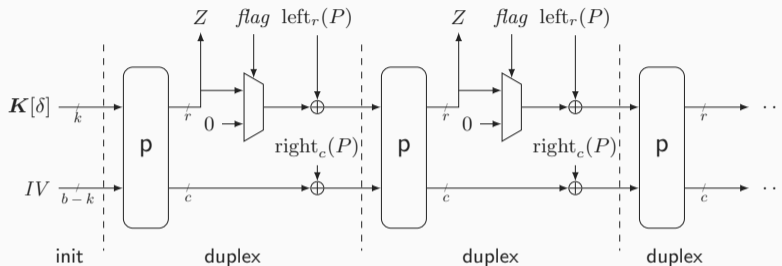
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Generalized Keyed Duplex



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- Basically the scheme of [DMV17] and [DM19], but:
 - including possible initial state rotation (not depicted)
 - yet another rephasing
- Security results of [DMV17] and [DM19] carry over
- First: understanding phasing and flagging

Generalized Keyed Duplex: Phasing



Generalized Keyed Duplex: Phasing

	A	P	S	A	P	S	A	P	S	A	...
[BDPV11a]	init			duplex			duplex			...	

- [BDPV11a]: duplex security reduced to sponge indistinguishability

Generalized Keyed Duplex: Phasing

	A	P	S	A	P	S	A	P	S	A	...
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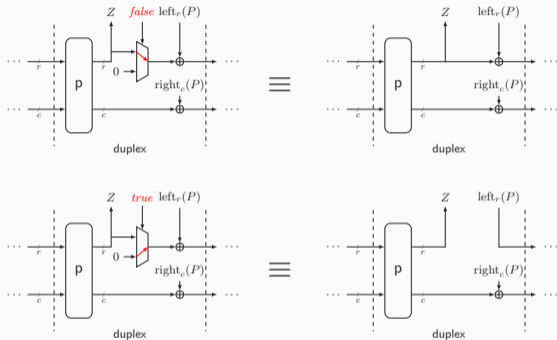
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Generalized Keyed Duplex: Phasing

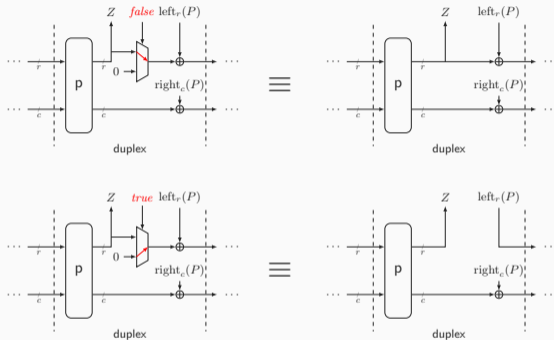
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[DM19]	init		duplex			duplex			...		
now	init	duplex			duplex			duplex			...

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- now: seemingly most useful phasing

Generalized Keyed Duplex: Flag (1)

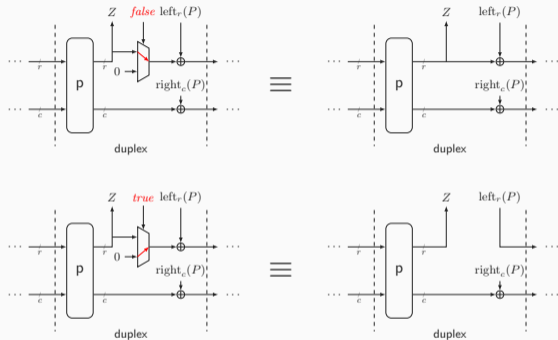


Generalized Keyed Duplex: Flag (1)



- Typical use case: authenticated encryption using duplex

Generalized Keyed Duplex: Flag (1)



- Typical use case: authenticated encryption using duplex
- Security decreases for increasing number of calls with *flag = true*
- Earlier P, p, Z phasing allowed outer part overwriting by default

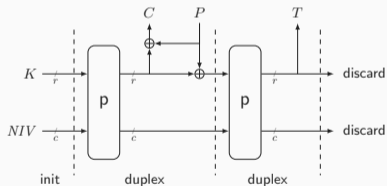
Generalized Keyed Duplex: Flag (2)

- Consider **extreme simplification of SpongeWrap** authenticated encryption
- Key K , plaintext P , ciphertext C , and tag T all r bits; nonce NIV c bits
- General case will be discussed later in this presentation

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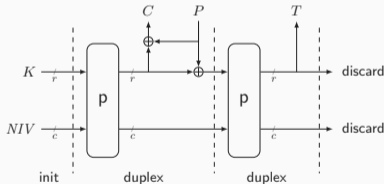
Encryption



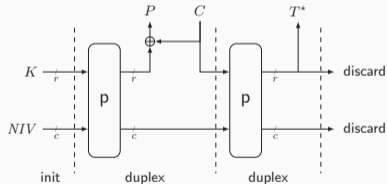
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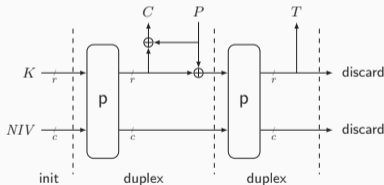
Decryption



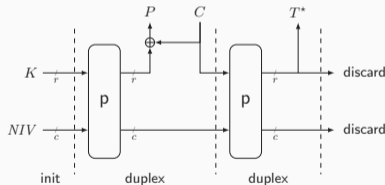
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Encryption



Decryption



- Duplex call with *flag = true* upon decryption
- Adversary can choose C and thus fix outer part to value of its choice

Understanding Duplex Security

Algorithm Keyed duplex construction $\text{KD}[p]_{\mathcal{K}}$

Interface: KD.init

Input: $(\delta, IV) \in \{1, \dots, \mu\} \times \mathcal{IV}$

Output: \emptyset

$S \leftarrow \text{rot}_{\alpha}(\mathbf{K}[\delta] \parallel IV)$

return \emptyset

Interface: KD.duplex

Input: $(\text{flag}, P) \in \{\text{true}, \text{false}\} \times \{0, 1\}^b$

Output: $Z \in \{0, 1\}^r$

$S \leftarrow p(S)$

$Z \leftarrow \text{left}_r(S)$

$S \leftarrow S \oplus [\text{flag}] \cdot (Z \parallel 0^{b-r}) \oplus P$

return Z

Security Model ([DMV17, DM19], with updated initial rotation and rephasing)

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$$\text{Adv}_{\text{KD}}(\text{D}) = \Delta_{\text{D}}(\text{KD}[p]_{\mathcal{K}}, p^{\pm}; \text{IXIF}[\text{ro}], p^{\pm})$$

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$$\text{Adv}_{\text{KD}}(\text{D}) = \Delta_{\text{D}}(\text{KD}[p]_{\mathcal{K}}, p^{\pm}; \text{IXIF}[\text{ro}], p^{\pm})$$

- $\text{IXIF}[\text{ro}]$ is basically random oracle in disguise
- If $\text{KD}[p]_{\mathcal{K}}$ is hard to distinguish from $\text{IXIF}[\text{ro}]$ for certain bound on adversarial resources, $\text{KD}[p]_{\mathcal{K}}$ roughly “behaves like” random oracle

Security Model ([DMV17, DM19], with updated initial rotation and rephasing)

Algorithm Keyed duplex construction $\text{KD}[p]_{\mathcal{K}}$

Interface: KD.init

Input: $(\delta, IV) \in \{1, \dots, \mu\} \times \mathcal{IV}$

Output: \emptyset

$S \leftarrow \text{rot}_{\alpha}(\mathbf{K}[\delta] \parallel IV)$

return \emptyset

Interface: KD.duplex

Input: $(\text{flag}, P) \in \{\text{true}, \text{false}\} \times \{0, 1\}^b$

Output: $Z \in \{0, 1\}^r$

$S \leftarrow p(S)$

$Z \leftarrow \text{left}_r(S)$

$S \leftarrow S \oplus [\text{flag}] \cdot (Z \parallel 0^{b-r}) \oplus P$

return Z

Algorithm Ideal extendable input function $\text{IXIF}[\text{ro}]$

Interface: IXIF.init

Input: $(\delta, IV) \in \{1, \dots, \mu\} \times \mathcal{IV}$

Output: \emptyset

$\text{path} \leftarrow \text{encode}[\delta] \parallel IV$

return \emptyset

Interface: IXIF.duplex

Input: $(\text{flag}, P) \in \{\text{true}, \text{false}\} \times \{0, 1\}^b$

Output: $Z \in \{0, 1\}^r$

$Z \leftarrow \text{ro}(\text{path}, r)$

$\text{path} \leftarrow \text{path} \parallel ([\text{flag}] \cdot (Z \parallel 0^{b-r}) \oplus P)$

return Z

$$\text{Adv}_{\text{KD}}(\text{D}) = \Delta_{\text{D}}(\text{KD}[p]_{\mathcal{K}}, p^{\pm}; \text{IXIF}[\text{ro}], p^{\pm})$$

- $\text{IXIF}[\text{ro}]$ is basically random oracle in disguise
- If $\text{KD}[p]_{\mathcal{K}}$ is hard to distinguish from $\text{IXIF}[\text{ro}]$ for certain bound on adversarial resources, $\text{KD}[p]_{\mathcal{K}}$ roughly “behaves like” random oracle
- Bound on adversarial resources is in turn determined by use case!

- M : data complexity (calls to construction)
- N : time complexity (calls to primitive)
- Q : number of init calls
- Q_{IV} : max # init calls for single IV
- L : # queries with repeated path (e.g., nonce-violation)
- Ω : # queries with overwriting outer part (e.g., RUP)
- $\nu_{r,c}^M$: some multicollision coefficient (often small)

Simplified Security Bound

$$\frac{Q_{IV}N}{2^k} + \frac{(L + \Omega + \nu_{r,c}^M)N}{2^c}$$

Security Bounds From [DMV17] and [DM19]

- M : data complexity (calls to construction)
- N : time complexity (calls to primitive)
- Q : number of init calls
- Q_{IV} : max # init calls for single IV
- L : # queries with repeated path (e.g., nonce-violation)
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- $\nu_{r,c}^M$: some multicollision coefficient (often small)

Simplified Security Bound

$$\frac{Q_{IV}N}{2^k} + \frac{(L + \Omega + \nu_{r,c}^M)N}{2^c}$$

Actual Security Bounds (Retained)

- [DMV17]:

$$\text{Adv}_{\text{KD}}(\text{D}) \leq \frac{(L + \Omega)N}{2^c} + \frac{2\nu_{r,c}^{2(M-L)}(N+1)}{2^c} + \frac{\binom{L+\Omega+1}{2}}{2^c} + \frac{(M-L-Q)Q}{2^{b-Q}} + \frac{M(M-L-1)}{2^b} + \frac{Q(M-L-Q)}{2^{\min\{c+k, \max\{b-\alpha, c\}\}}} + \frac{Q_{IV}N}{2^k} + \frac{\binom{\mu}{2}}{2^k}$$

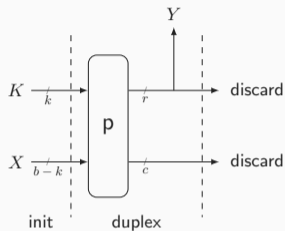
- [DM19] (with one simplification):

$$\text{Adv}_{\text{KD}}(\text{D}) \leq \frac{(L + \Omega)N}{2^c} + \frac{2\nu_{r,c}^M(N+1)}{2^c} + \frac{\nu_{r,c}^M(L + \Omega) + \binom{L+\Omega}{2}}{2^c} + \frac{\binom{M-L-Q}{2} + (M-L-Q)(L + \Omega)}{2^b} + \frac{\binom{M+N}{2} + \binom{N}{2}}{2^b} + \frac{Q(M-Q)}{2^{\min\{c+k, \max\{b-\alpha, c\}\}}} + \frac{Q_{IV}N}{2^k} + \frac{\binom{\mu}{2}}{2^k}$$

Intermezzo: Multicollision Coefficient (Skipped)

Use Case 1: Truncated Permutation

Truncated Permutation



Algorithm Truncated permutation $TP[p]$

Input: $(K, X) \in \{0, 1\}^k \times \{0, 1\}^{b-k}$

Output: $Y \in \{0, 1\}^r$

Underlying keyed duplex: $KD[p]_{(K)}$

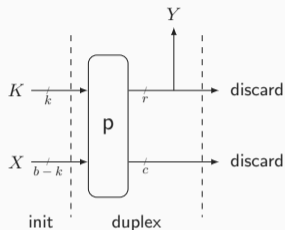
$KD.init(1, X)$

$Y \leftarrow KD.duplex(false, 0^b)$

return Y

- PRP-to-PRF conversion: SoP/EDM/EDMD/truncation/STH/...

Truncated Permutation



Algorithm Truncated permutation $TP[p]$

Input: $(K, X) \in \{0, 1\}^k \times \{0, 1\}^{b-k}$

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Underlying keyed duplex: $KD[p]_{(K)}$

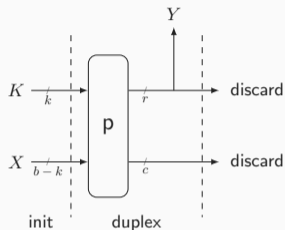
$KD.init(1, X)$

$Y \leftarrow KD.duplex(false, 0^b)$

return Y

- PRP-to-PRF conversion: SoP/EDM/EDMD/truncation/STH/...
- Trend towards RP-to-PRF conversion:
 - Sum of externally keyed permutations [CLM19]
 - Permutation-based EDM [DNT21]

Truncated Permutation



Algorithm Truncated permutation $TP[p]$

Input: $(K, X) \in \{0, 1\}^k \times \{0, 1\}^{b-k}$

Output: $Y \in \{0, 1\}^r$

Underlying keyed duplex: $KD[p]_{(K)}$

$KD.init(1, X)$

$Y \leftarrow KD.duplex(false, 0^b)$

return Y

- PRP-to-PRF conversion: SoP/EDM/EDMD/truncation/STH/...
- Trend towards RP-to-PRF conversion:
 - Sum of externally keyed permutations [CLM19]
 - Permutation-based EDM [DNT21]
- Truncation of externally keyed permutation **can be described using duplex**

Truncated Permutation: Security (1)

- Consider distinguisher D against PRF security of $TP[p]$

$$\mathbf{Adv}_{TP}^{\text{prf}}(D) = \Delta_D \left(TP[p]_{K, p^\pm} ; R^{\text{prf}}, p^\pm \right)$$

- D can make q construction queries + N primitive queries

Truncated Permutation: Security (1)

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$$\mathbf{Adv}_{TP}^{\text{prf}}(D) = \Delta_D \left(TP[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right)$$

- D can make q construction queries + N primitive queries
- $TP[p]_K$ is basically just $TP[KD[p]_K]$

Truncated Permutation: Security (1)

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$$\mathbf{Adv}_{TP}^{\text{prf}}(D) = \Delta_D \left(TP[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right)$$

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- $TP[p]_K$ is basically just $TP[KD[p]_K]$
- Triangle inequality:

$$\begin{aligned} \mathbf{Adv}_{TP}^{\text{prf}}(D) &= \Delta_D \left(TP[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right) \\ &= \Delta_D \left(TP[KD[p]_K], p^\pm ; R^{\text{prf}}, p^\pm \right) \\ &\leq \Delta_D \left(TP[KD[p]_K], p^\pm ; TP[IXIF[ro]], p^\pm \right) + \Delta_D \left(TP[IXIF[ro]], p^\pm ; R^{\text{prf}}, p^\pm \right) \end{aligned}$$

Truncated Permutation: Security (1)

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$$\mathbf{Adv}_{TP}^{\text{prf}}(D) = \Delta_D \left(TP[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right)$$

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Truncated Permutation: Security (1)

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$$\mathbf{Adv}_{TP}^{\text{prf}}(D) = \Delta_D \left(TP[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right)$$

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- Triangle inequality:

$$\begin{aligned} \mathbf{Adv}_{TP}^{\text{prf}}(D) &= \Delta_D \left(TP[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right) \\ &= \Delta_D \left(TP[KD[p]_K], p^\pm ; R^{\text{prf}}, p^\pm \right) \\ &\leq \Delta_D \left(TP[KD[p]_K], p^\pm ; TP[IXIF[ro]], p^\pm \right) + \Delta_D \left(TP[IXIF[ro]], p^\pm ; R^{\text{prf}}, p^\pm \right) \\ &\quad \curvearrowright \leq \Delta_{D'} \left(KD[p]_K, p^\pm ; IXIF[ro], p^\pm \right) \quad \curvearrowright = 0 \end{aligned}$$

Truncated Permutation: Security (1)

- Consider distinguisher D against PRF security of $TP[p]$

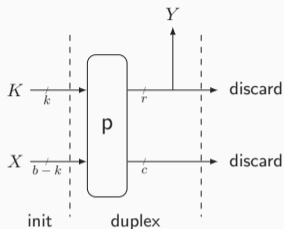
$$\mathbf{Adv}_{TP}^{\text{prf}}(D) = \Delta_D \left(TP[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right)$$

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$$\begin{aligned} \mathbf{Adv}_{TP}^{\text{prf}}(D) &= \Delta_D \left(TP[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right) \\ &= \Delta_D \left(TP[KD[p]_K], p^\pm ; R^{\text{prf}}, p^\pm \right) \\ &\leq \Delta_D \left(TP[KD[p]_K], p^\pm ; TP[IXIF[ro]], p^\pm \right) + \Delta_D \left(TP[IXIF[ro]], p^\pm ; R^{\text{prf}}, p^\pm \right) \\ &\quad \curvearrowright \leq \Delta_{D'} \left(KD[p]_K, p^\pm ; IXIF[ro], p^\pm \right) \quad \curvearrowright = 0 \end{aligned}$$

- What are the resources of D' ?

Truncated Permutation: Security (2)



Algorithm Truncated permutation $TP[p]$

Input: $(K, X) \in \{0, 1\}^k \times \{0, 1\}^{b-k}$

Output: $Y \in \{0, 1\}^r$

Underlying keyed duplex: $KD[p]_{(K)}$

$KD.init(1, X)$

$Y \leftarrow KD.duplex(false, 0^b)$

return Y

resources of D'

in terms of resources of D

M : data complexity (calls to construction)

N : time complexity (calls to primitive)

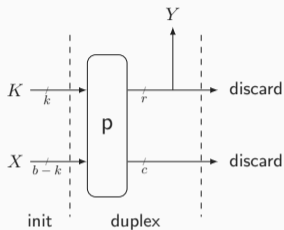
Q : number of init calls

Q_{IV} : max # init calls for single IV

L : # queries with repeated path

Ω : # queries with overwriting outer part

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in terms of resources of D

M : data complexity (calls to construction)

N : time complexity (calls to primitive)

$\longrightarrow N$

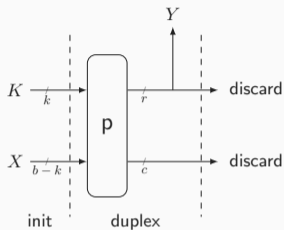
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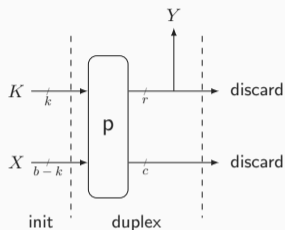
$KD.init(1, X)$

$Y \leftarrow KD.duplex(false, 0^b)$

return Y

resources of D'	in terms of	resources of D
M : data complexity (calls to construction)	\longrightarrow	q
N : time complexity (calls to primitive)	\longrightarrow	N
Q : number of init calls	\longrightarrow	q
Q_{IV} : max # init calls for single IV		
L : # queries with repeated path		
Ω : # queries with overwriting outer part		

Truncated Permutation: Security (2)



Algorithm Truncated permutation $TP[p]$

Input: $(K, X) \in \{0, 1\}^k \times \{0, 1\}^{b-k}$

Output: $Y \in \{0, 1\}^r$

Underlying keyed duplex: $KD[p]_{(K)}$

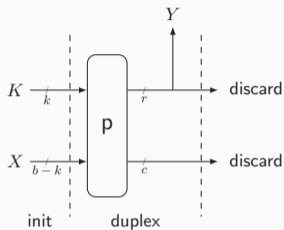
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return Y

resources of D'	in terms of	resources of D
M : data complexity (calls to construction)	\longrightarrow	q
N : time complexity (calls to primitive)	\longrightarrow	N
Q : number of init calls	\longrightarrow	q
Q_{IV} : max # init calls for single IV	\longrightarrow	1
L : # queries with repeated path		
Ω : # queries with overwriting outer part		

Truncated Permutation: Security (2)



Algorithm Truncated permutation TP[p]

Input: $(K, X) \in \{0, 1\}^k \times \{0, 1\}^{b-k}$

Output: $Y \in \{0, 1\}^r$

Underlying keyed duplex: $\text{KD}[p]_{(K)}$

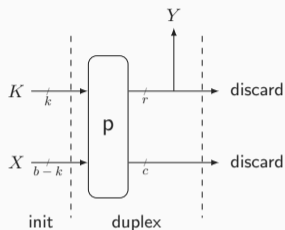
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resources of D'	in terms of	resources of D
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Truncated Permutation: Security (2)



Algorithm Truncated permutation $TP[p]$

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Output: $Y \in \{0, 1\}^r$

Underlying keyed duplex: $KD[p]_{(K)}$

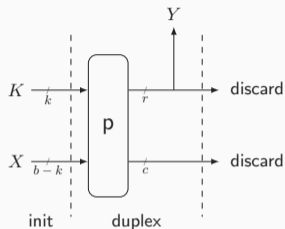
$KD.init(1, X)$

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resources of D'	in terms of	resources of D
M : data complexity (calls to construction)	\longrightarrow	q
N : time complexity (calls to primitive)	\longrightarrow	N
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Truncated Permutation: Security (2)



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Output: $Y \in \{0, 1\}^r$

Underlying keyed duplex: $\text{KD}[p]_{(K)}$

$\text{KD.init}(1, X)$

$Y \leftarrow \text{KD.duplex}(\text{false}, 0^b)$

return Y

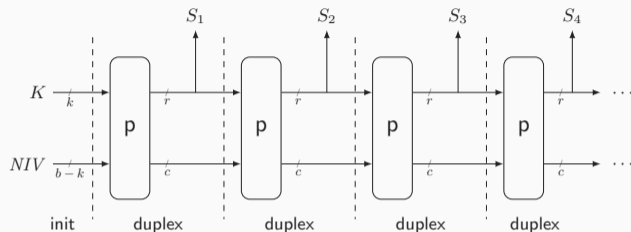
resources of D'	in terms of	resources of D
M : data complexity (calls to construction)	\longrightarrow	q
N : time complexity (calls to primitive)	\longrightarrow	N
Q : number of init calls	\longrightarrow	q
Q_{IV} : max # init calls for single IV	\longrightarrow	1
L : # queries with repeated path	\longrightarrow	0
Ω : # queries with overwriting outer part	\longrightarrow	0

From [DMV17] (in single-user setting): $\text{Adv}_{\text{KD}}(D') \leq \frac{2\nu_{r,c}^{2q}(N+1)}{2^c} + \frac{2\binom{q}{2}}{2^b} + \frac{N}{2^k}$

Use Case 2: Parallel Keystream Generation (Skipped)

Use Case 3: Sequential Keystream Generation

Sequential Keystream Generation



- Input: key K , nonce NIV
- Output: keystream S of requested length

Algorithm Sequential keystream generation S-SC[p]

Input: $(K, NIV, \ell) \in \{0, 1\}^k \times \{0, 1\}^{b-k} \times \mathbb{N}$

Output: $S \in \{0, 1\}^\ell$

Underlying keyed duplex: $KD[p]_{(K)}$

$S \leftarrow \emptyset$

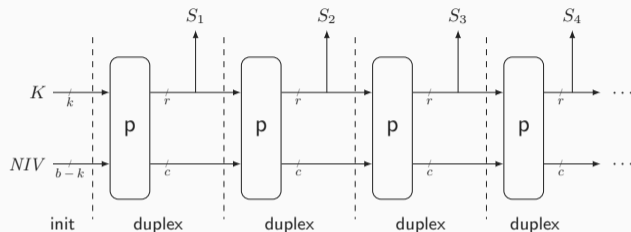
$KD.init(1, NIV)$

for $i = 1, \dots, \lceil \ell/r \rceil$ **do**

$S \leftarrow S \parallel KD.duplex(false, 0^b)$

return $left_\ell(S)$

Sequential Keystream Generation



- Input: key K , nonce NIV
- Output: keystream S of requested length
- PRF security of S-SC[p]:
 - Comparable analysis as for TP[p]

Algorithm Sequential keystream generation S-SC[p]

Input: $(K, NIV, \ell) \in \{0, 1\}^k \times \{0, 1\}^{b-k} \times \mathbb{N}$

Output: $S \in \{0, 1\}^\ell$

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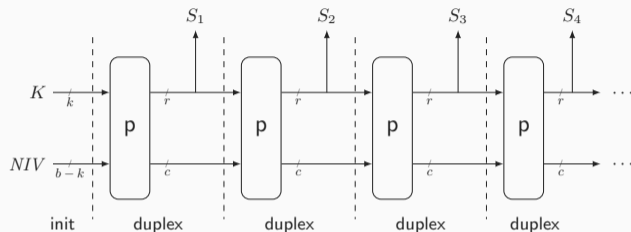
$\text{KD.init}(1, NIV)$

for $i = 1, \dots, \lceil \ell/r \rceil$ **do**

$S \leftarrow S \parallel \text{KD.duplex}(\text{false}, 0^b)$

return $\text{left}_\ell(S)$

Sequential Keystream Generation



- Input: key K , nonce NIV
- Output: keystream S of requested length
- PRF security of S-SC[p]:
 - Comparable analysis as for TP[p]
 - Resources of D' slightly differ

Algorithm Sequential keystream generation S-SC[p]

Input: $(K, NIV, \ell) \in \{0, 1\}^k \times \{0, 1\}^{b-k} \times \mathbb{N}$

Output: $S \in \{0, 1\}^\ell$

Underlying keyed duplex: $KD[p]_{(K)}$

$S \leftarrow \emptyset$

$KD.init(1, NIV)$

for $i = 1, \dots, \lceil \ell/r \rceil$ **do**

$S \leftarrow S \parallel KD.duplex(false, 0^b)$

return $left_\ell(S)$

Sequential Keystream Generation: Security

- Consider distinguisher D against PRF security of $S\text{-SC}[p]$

$$\mathbf{Adv}_{S\text{-SC}}^{\text{prf}}(D) = \Delta_D \left(S\text{-SC}[p]_{K, p^\pm} ; R^{\text{prf}}, p^\pm \right)$$

- D can make q construction queries (total σ blocks) + N primitive queries

Sequential Keystream Generation: Security

- Consider distinguisher D against PRF security of $S\text{-SC}[p]$

$$\mathbf{Adv}_{S\text{-SC}}^{\text{prf}}(D) = \Delta_D \left(S\text{-SC}[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right)$$

- D can make q construction queries (total σ blocks) + N primitive queries
- Triangle inequality: $\mathbf{Adv}_{S\text{-SC}}^{\text{prf}}(D) \leq \Delta_{D'}(KD[p]_K, p^\pm ; \text{IXIF}[ro], p^\pm)$

Sequential Keystream Generation: Security

- Consider distinguisher D against PRF security of $S\text{-SC}[p]$

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- Triangle inequality: $\mathbf{Adv}_{S\text{-SC}}^{\text{prf}}(D) \leq \Delta_{D'}(KD[p]_K, p^\pm ; \text{IXIF}[ro], p^\pm)$
- What are the resources of D' ?

Sequential Keystream Generation: Security

- Consider distinguisher D against PRF security of $S\text{-SC}[p]$

$$\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) = \Delta_D \left(S\text{-SC}[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right)$$

- D can make q construction queries (total σ blocks) + N primitive queries
- Triangle inequality: $\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) \leq \Delta_{D'}(KD[p]_K, p^\pm ; \text{IXIF}[ro], p^\pm)$
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resources of D'	in terms of	resources of D
M : data complexity (calls to construction)		
N : time complexity (calls to primitive)		
Q : number of init calls		
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L : # queries with repeated path		
Ω : # queries with overwriting outer part		

Sequential Keystream Generation: Security

- Consider distinguisher D against PRF security of $S\text{-SC}[p]$

$$\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) = \Delta_D \left(S\text{-SC}[p]_{K, p^\pm} ; R^{\text{prf}}, p^\pm \right)$$

- D can make q construction queries (total σ blocks) + N primitive queries
- Triangle inequality: $\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) \leq \Delta_{D'}(KD[p]_{K, p^\pm} ; IXIF[ro], p^\pm)$
- What are the resources of D' ?

resources of D'	in terms of	resources of D
M : data complexity (calls to construction)		
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Q_{IV} : max # init calls for single IV		
L : # queries with repeated path		
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Sequential Keystream Generation: Security

- Consider distinguisher D against PRF security of $S\text{-SC}[p]$

$$\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) = \Delta_D \left(S\text{-SC}[p]_{K, p^\pm} ; R^{\text{prf}}, p^\pm \right)$$

- D can make q construction queries (total σ blocks) + N primitive queries
- Triangle inequality: $\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) \leq \Delta_{D'}(KD[p]_{K, p^\pm} ; \text{IXIF}[\text{ro}], p^\pm)$
- What are the resources of D' ?

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Sequential Keystream Generation: Security

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- Triangle inequality: $\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) \leq \Delta_{D'}(KD[p]_{K, p^\pm} ; \text{IXIF}[\text{ro}], p^\pm)$
- What are the resources of D' ?

resources of D'	in terms of	resources of D
M : data complexity (calls to construction)	\longrightarrow	σ
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L : # queries with repeated path	\longrightarrow	0
Ω : # queries with overwriting outer part	\longrightarrow	0

Sequential Keystream Generation: Security

- Consider distinguisher D against PRF security of $S\text{-SC}[p]$

$$\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) = \Delta_D \left(S\text{-SC}[p]_K, p^\pm ; R^{\text{prf}}, p^\pm \right)$$

- D can make q construction queries (total σ blocks) + N primitive queries
- Triangle inequality: $\text{Adv}_{S\text{-SC}}^{\text{prf}}(D) \leq \Delta_{D'}(KD[p]_K, p^\pm ; \text{XIF}[ro], p^\pm)$
- What are the resources of D' ?

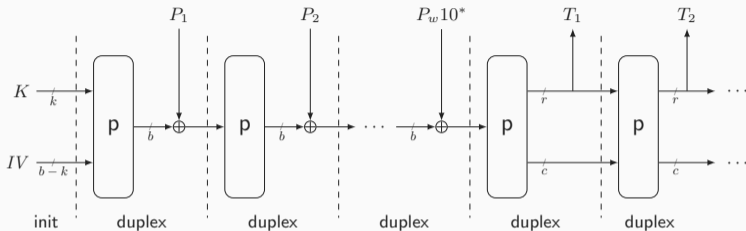
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From [DMV17] (in single-user setting):

$$\text{Adv}_{\text{KD}}(D') \leq \frac{2\nu_{r,c}^{2\sigma}(N+1)}{2^c} + \frac{(\sigma-q)q}{2^{b-q}} + \frac{2\binom{\sigma}{2}}{2^b} + \frac{q(\sigma-q)}{2^{\min\{c+k,b\}}} + \frac{N}{2^k}$$

Use Case 4: Message Authentication

Full-State Keyed Sponge [BDPV12]



- Input: key K , initial value IV , message P
- Output: tag T

Algorithm Full-state keyed sponge FSKS[p]

Input: $(K, IV, P) \in \{0, 1\}^k \times \mathcal{IV} \times \{0, 1\}^*$

Output: $T \in \{0, 1\}^t$

Underlying keyed duplex: $\text{KD}[p]_{(K)}$

$(P_1, P_2, \dots, P_w) \leftarrow \text{pad}_b^{10^*}(P)$

$T \leftarrow \emptyset$

$\text{KD.init}(1, IV)$

for $i = 1, \dots, w$ **do**

$\text{KD.duplex}(\text{false}, P_i)$

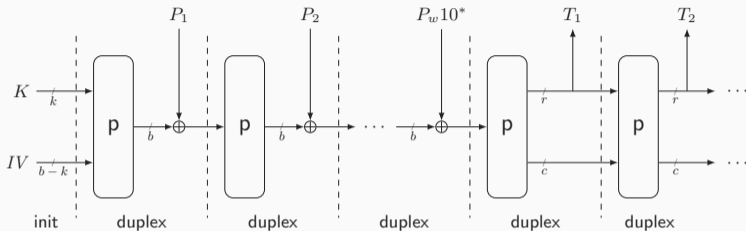
 ▷ discard output

for $i = 1, \dots, \lceil t/r \rceil$ **do**

$T \leftarrow T \parallel \text{KD.duplex}(\text{false}, 0^b)$

return $\text{left}_t(T)$

Full-State Keyed Sponge [BDPV12]



- Input: key K , initial value IV , message P
- Output: tag T
- Analysis of [MRV15] applies

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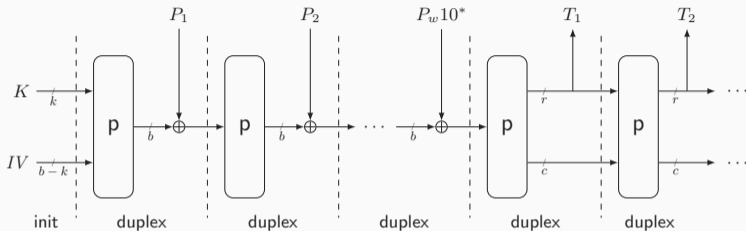
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- Input: key K , initial value IV , message P
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- PRF security of $\text{FSKS}[p]$:
 - Comparable analysis as for $\text{S-SC}[p]$

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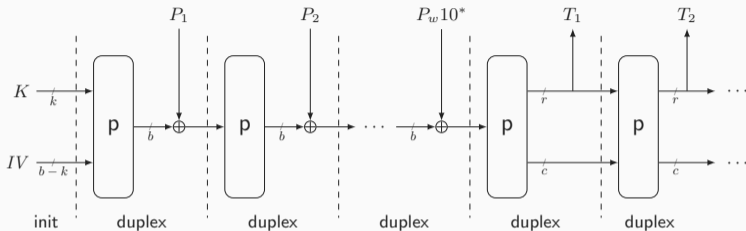
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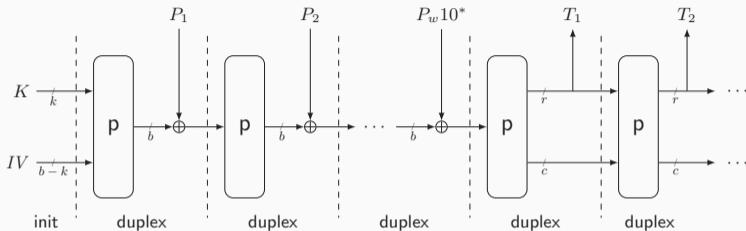
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 - **Impacts resources of D'**

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$$\text{Adv}_{\text{FSKS}}^{\text{prf}}(D) = \Delta_D \left(\text{FSKS}[p]_{K, p^\pm} ; \text{R}^{\text{prf}}, p^\pm \right)$$

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Full-State Keyed Sponge: Security

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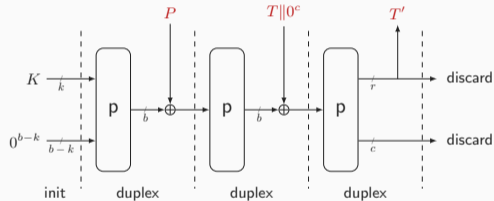
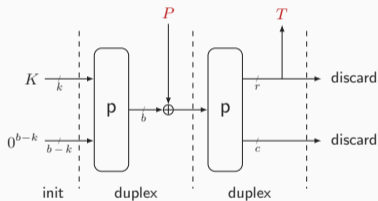
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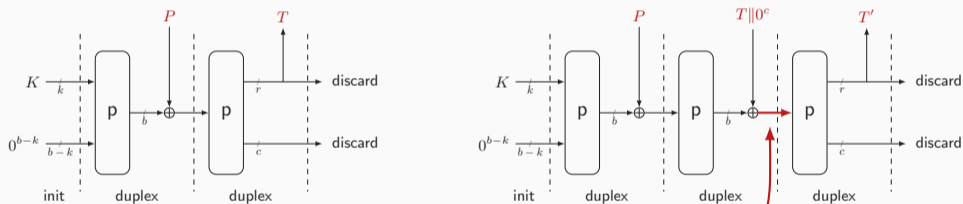
Full-State Keyed Sponge: Adversarial Power in Influencing Outer Part

- Repeated paths (i.e., large L) can **seriously affect security**
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Full-State Keyed Sponge: Adversarial Power in Influencing Outer Part

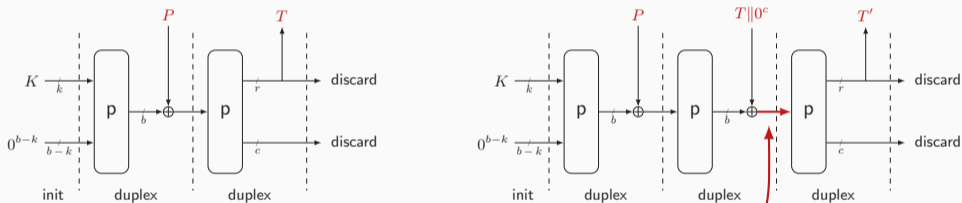
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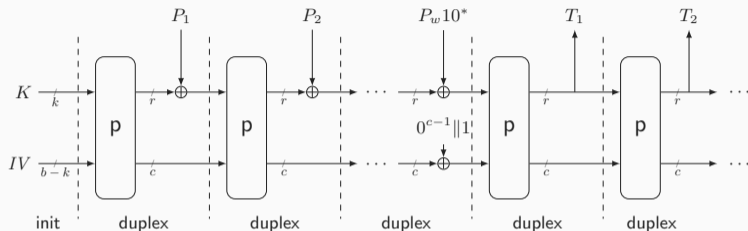
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- State of second query before squeezing equals $0^r \parallel *^c$
- Key recovery attack:
 - Make q twin queries as above and N primitive queries of form $0^r \parallel *^c$
 - Construction-primitive collision (likely if $\frac{q \cdot N}{2^c} \approx 1$) \rightarrow **derive K**



- Input: key K , initial value IV , message P
- Output: tag T

Algorithm Ascon-PRF[p]

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$\text{KD.init}(1, IV)$

for $i = 1, \dots, w - 1$ **do**

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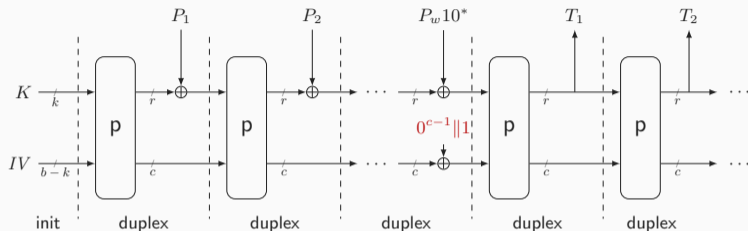
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- **Domain separation** solves problem of repeated paths

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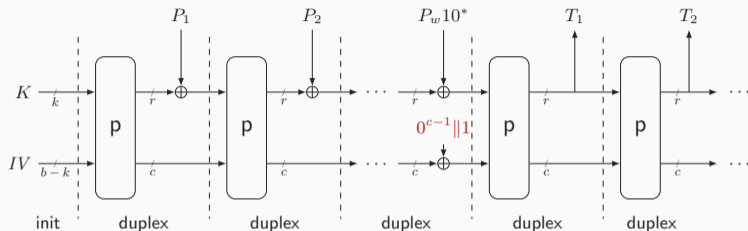
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 - Repeated paths may still occur...

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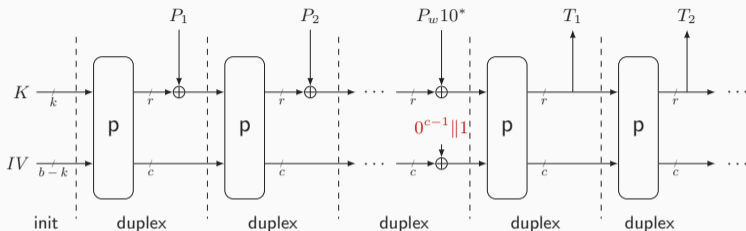
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- Input: key K , initial value IV , message P
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 - Repeated paths may still occur...
 - ... but adversary cannot exploit them

Algorithm Ascon-PRF[p]

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- Improved bound from [DMV17]:
 - Loose bounding in original proof
 - Resolving this loose bounding makes $\frac{(q-1)N + \binom{q}{2}}{2^c}$ vanish

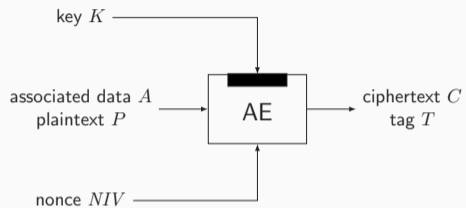
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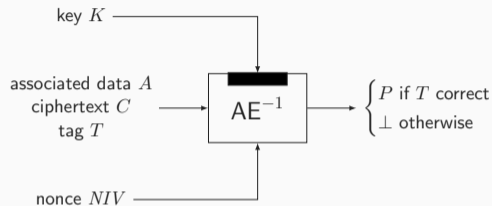
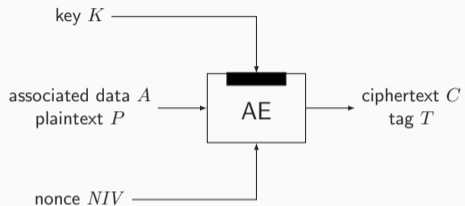
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- Improved bound from [DM19]:
 - Defines additional parameter $\nu_{\text{fix}} \leq L + \Omega$
 - In most cases $\nu_{\text{fix}} = L + \Omega$; for current case $\nu_{\text{fix}} = 0$
 - Dominant term $\frac{(q-1)N + \binom{q}{2}}{2^c}$ never appears in the first place

Use Case 5: Authenticated Encryption (Shortened)

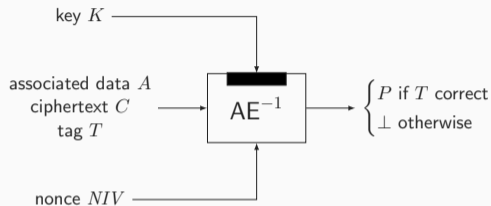
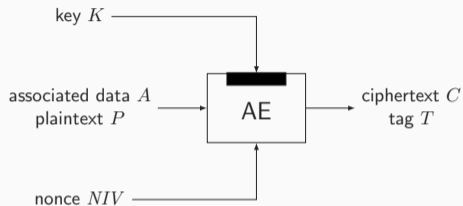
Authenticated Encryption



Authenticated Encryption



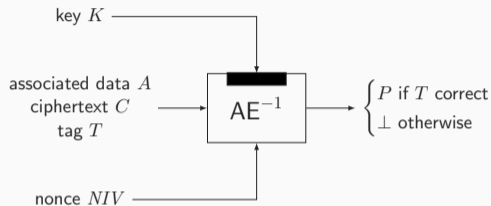
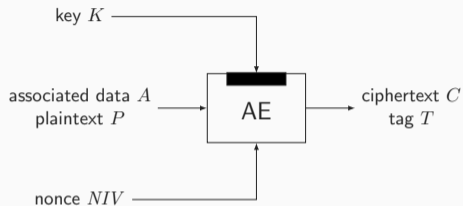
Authenticated Encryption



Role of Duplex

- Blockwise construction allows for processing different types of in-/output

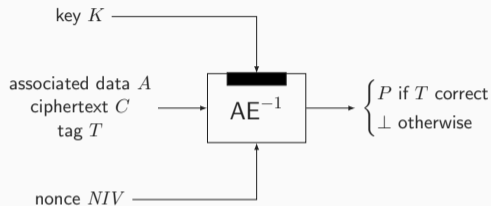
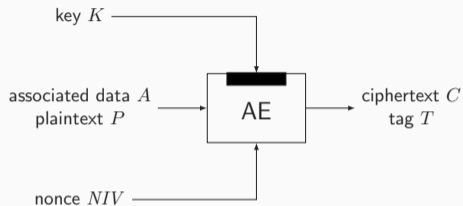
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Role of Duplex

- Blockwise construction allows for processing different types of in-/output
- Usage of flag makes duplex-style encryption decryptable

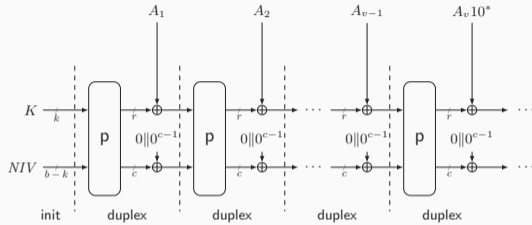
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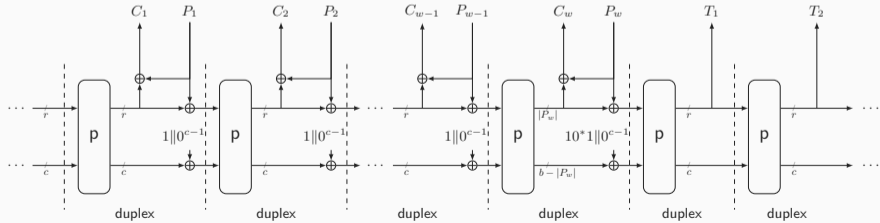
Role of Duplex

- Blockwise construction allows for processing different types of in-/output
- Usage of flag makes duplex-style encryption decryptable
(Although the flag is not a necessity for this)

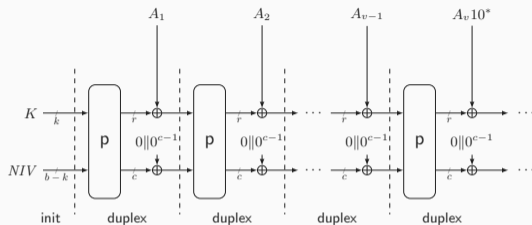
MonkeySpongeWrap: Encryption



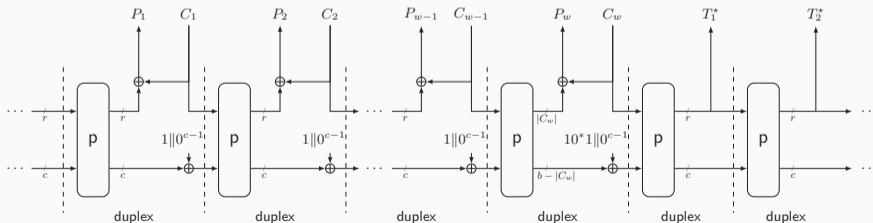
- State initialized using key and nonce
- Cleaned-up and synchronized domain separation
- Spill-over into inner part
- Used in Xoodyak and Gimli (a.o.)



MonkeySpongeWrap: Decryption



- Decryption similar to encryption
- Notable difference:
 - Processing of C
 - Duplexing with *flag = true*



- Consider distinguisher D against AE security of MonkeySpongeWrap[p]

$$\mathbf{Adv}_{\text{MonkeySpongeWrap}}^{\text{ae}}(D) = \Delta_D(\text{ENC}[p]_K, \text{DEC}[p]_K, p^\pm ; R^{\text{ae}}, \perp, p^\pm)$$

- D can make: q_e encryption queries (total σ_e blocks),
 D can make: q_d decryption queries (total σ_d blocks),
 D can make: N primitive queries

MonkeySpongeWrap: Security (1)

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- Triangle inequality derivation slightly more involved than before:

$$\mathbf{Adv}_{\text{MonkeySpongeWrap}}^{\text{ae}}(D) \leq \Delta_{D'}(\text{KD}[p]_K, p^\pm; \text{IXIF}[\text{ro}], p^\pm) + \frac{q_d}{2^t}$$

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- *What are the resources of D' ?*

MonkeySpongeWrap: Security (2)

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resources of D'	in terms of	resources of D
M : data complexity (calls to construction)		
N : time complexity (calls to primitive)	\longrightarrow	N
Q : number of init calls		
Q_{IV} : max # init calls for single IV		
L : # queries with repeated path		
Ω : # queries with overwriting outer part		

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From [DMV17] (in single-user setting):

$$\text{Adv}_{\text{KD}}(D') \leq \frac{2\nu_{r,c}^{2\sigma}(N+1)}{2^c} + \frac{\sigma_d N + \binom{\sigma_d}{2}}{2^c} + \frac{(\sigma-q)q}{2^{b-q}} + \frac{2\binom{\sigma}{2}}{2^b} + \frac{q(\sigma-q)}{2^{\min\{c+k,b\}}} + \frac{N}{2^k}$$

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attack of Gilbert et al. [GHKR23] “operates” here, with $\sigma_d, N \approx 2^{3c/4}$

Conclusion

Generalized Keyed Duplex

- Versatile construction but application not always clear
- Five representative use cases
- Further use cases: PRNG, PBKDF, ...
- Generic security of ISAP v2 follows from duplex and SuKS [DEM⁺20]
- Caution: all presented results only hold in **random permutation model**

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Much More in Paper

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- Application of bounds of both [DMV17] and [DM19] to use cases
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Thank you for your attention!

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Supporting Slides

Intermezzo: Multicollision Coefficient

Definition

- M balls, 2^r bins
- $\nu_{r,c}^M$ is smallest x such that $\Pr(|\text{fullest bin}| > x) \leq \frac{x}{2^c}$

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- Denote this maximum by ν

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- However, if we take $\nu = \nu_{r,c}^M$, this happens with probability at most $\frac{\nu}{2^c}$

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- However, if we take $\nu = \nu_{r,c}^M$, this happens with probability at most $\frac{\nu}{2^c}$
- This term is negligible compared to the main probability bound

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- If $M \gg 2^r$, there will likely be a bin with around $\text{linear}(b) \cdot \frac{M}{2^r}$ balls

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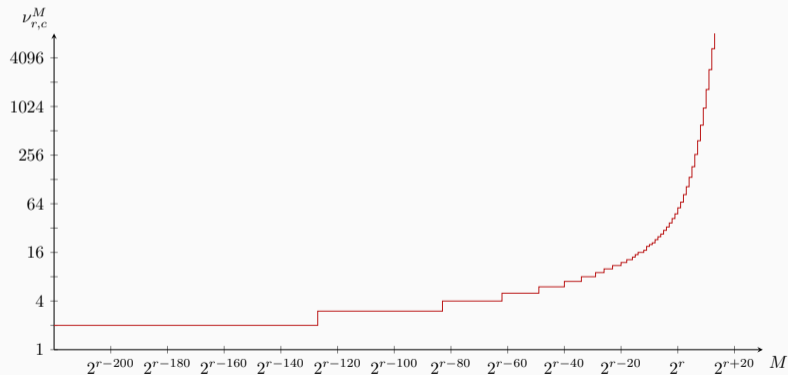
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- If $M \gg 2^r$, there will likely be a bin with around $\text{linear}(b) \cdot \frac{M}{2^r}$ balls
- Formula for $\nu_{r,c}^M$, and upper bounds in above 2 cases, derived in [DMV17]
- $\nu_{r,c}^M$ is (at most) smallest x that satisfies

$$\frac{2^b e^{-M/2^r} (M/2^r)^x}{(x - M/2^r)x!} \leq 1$$

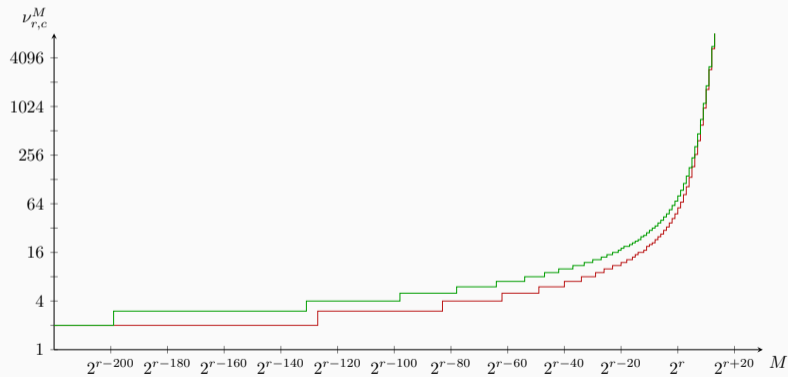
Stairway to Heaven for $b = 256$



$M/2^r$	$\nu_{r,c}^M$
2^{-256}	—
2^{-128}	2
2^{-64}	4
2^{-32}	8
2^{-16}	14
2^{-8}	23
2^0	57
2^8	601
2^{16}	70205
2^{19}	537313

Intermezzo: Multicollision Coefficient $\nu_{r,c}^M$ (3)

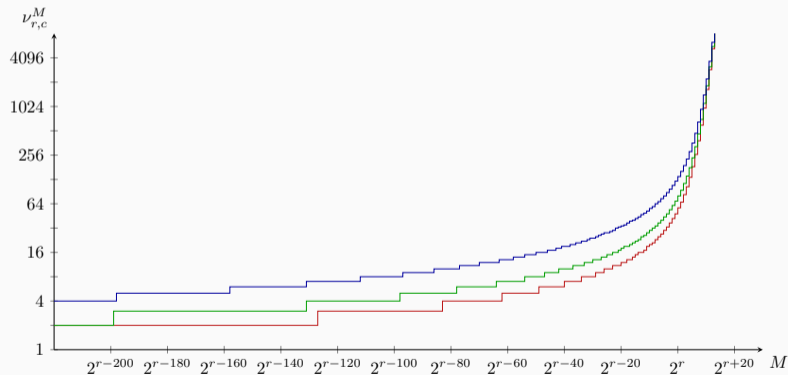
Stairway to Heaven for $b = 256$, $b = 400$



$M/2^r$	$\nu_{r,c}^M$	$\nu_{r,c}^M$
2^{-256}	—	2
2^{-128}	2	4
2^{-64}	4	7
2^{-32}	8	12
2^{-16}	14	21
2^{-8}	23	34
2^0	57	80
2^8	601	707
2^{16}	70205	71484
2^{19}	537313	540887

Intermezzo: Multicollision Coefficient $\nu_{r,c}^M$ (3)

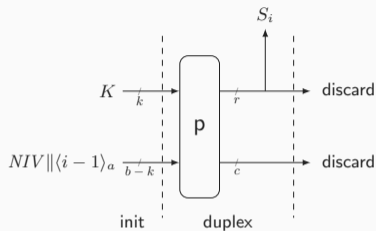
Stairway to Heaven for $b = 256$, $b = 400$, $b = 800$



$M/2^r$	$\nu_{r,c}^M$	$\nu_{r,c}^M$	$\nu_{r,c}^M$
2^{-256}	—	2	4
2^{-128}	2	4	7
2^{-64}	4	7	12
2^{-32}	8	12	23
2^{-16}	14	21	40
2^{-8}	23	34	64
2^0	57	80	139
2^8	601	707	944
2^{16}	70205	71484	74119
2^{19}	537313	540887	548194

Use Case 2: Parallel Keystream Generation

Parallel Keystream Generation



- Input: key K , nonce NIV
- Output: keystream S of requested length

Algorithm Parallel keystream generation P-SC[p]

Input: $(K, NIV, \ell) \in \{0, 1\}^k \times \{0, 1\}^{b-k-a} \times \{0, \dots, r2^a\}$

Output: $S \in \{0, 1\}^\ell$

Underlying keyed duplex: $KD[p]_{(K)}$

$S \leftarrow \emptyset$

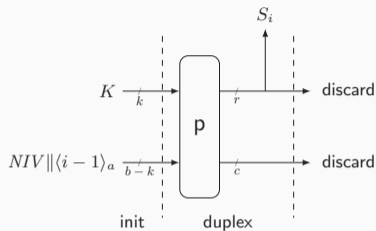
for $i = 1, \dots, \lceil \ell/r \rceil$ **do**

$KD.init(1, NIV \parallel \langle i-1 \rangle_a)$

$S \leftarrow S \parallel KD.duplex(false, 0^b)$

return $left_\ell(S)$

Parallel Keystream Generation



- Input: key K , nonce NIV
- Output: keystream S of requested length
- P-SC[p] can be seen as TP[p] in counter mode

Algorithm Parallel keystream generation P-SC[p]

Input: $(K, NIV, \ell) \in \{0, 1\}^k \times \{0, 1\}^{b-k-a} \times \{0, \dots, r2^a\}$

Output: $S \in \{0, 1\}^\ell$

Underlying keyed duplex: $KD[p]_{(K)}$

$S \leftarrow \emptyset$

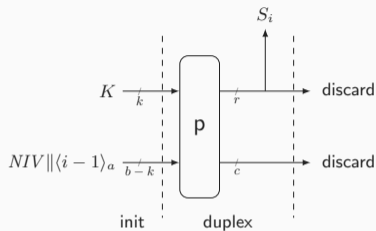
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Parallel Keystream Generation



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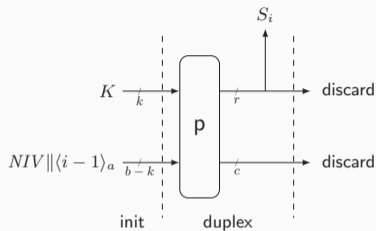
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- Input: key K , nonce NIV
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- P-SC[p] can be seen as TP[p] in counter mode
- PRF security of P-SC[p] easily follows:

Parallel Keystream Generation



Algorithm Parallel keystream generation P-SC[p]

Input: $(K, NIV, \ell) \in \{0, 1\}^k \times \{0, 1\}^{b-k-a} \times \{0, \dots, r2^a\}$

Output: $S \in \{0, 1\}^\ell$

Underlying keyed duplex: $KD[p]_{(K)}$

$S \leftarrow \emptyset$

for $i = 1, \dots, \lceil \ell/r \rceil$ **do**

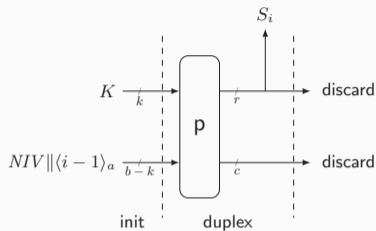
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- P-SC[p] can be seen as TP[p] in counter mode
- PRF security of P-SC[p] easily follows:
 - TP[p] behaves like a PRF (up to good bound)

Parallel Keystream Generation



Algorithm Parallel keystream generation P-SC[p]

Input: $(K, NIV, \ell) \in \{0, 1\}^k \times \{0, 1\}^{b-k-a} \times \{0, \dots, r2^a\}$

Output: $S \in \{0, 1\}^\ell$

Underlying keyed duplex: $KD[p]_{(K)}$

$S \leftarrow \emptyset$

for $i = 1, \dots, \lceil \ell/r \rceil$ **do**

$KD.init(1, NIV \parallel \langle i-1 \rangle_a)$

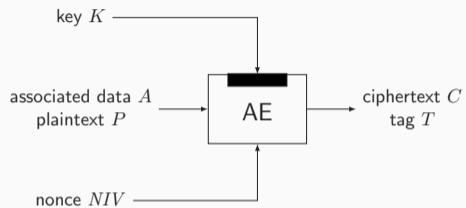
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return $left_\ell(S)$

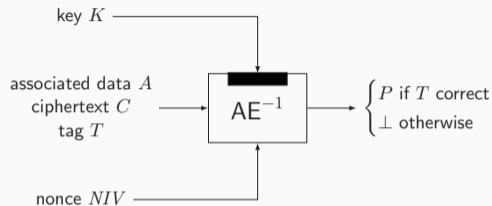
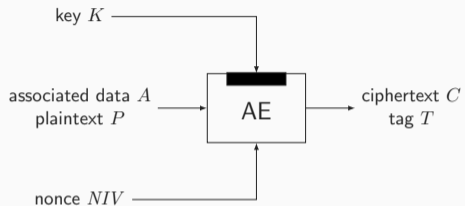
- Input: key K , nonce NIV
- Output: keystream S of requested length
- P-SC[p] can be seen as TP[p] in counter mode
- PRF security of P-SC[p] easily follows:
 - TP[p] behaves like a PRF (up to good bound)
 - Counter mode with a PRF generates uniform random keystream (provided nonce/counter never repeats)

Use Case 5: Authenticated Encryption

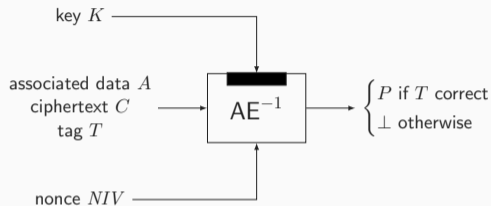
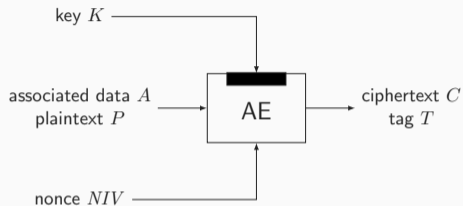
Authenticated Encryption



Authenticated Encryption



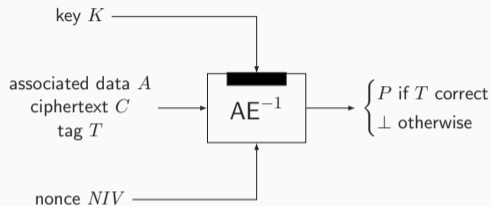
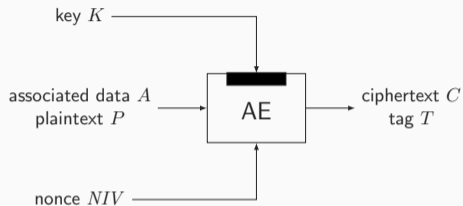
Authenticated Encryption



Role of Duplex

- Blockwise construction allows for processing different types of in-/output

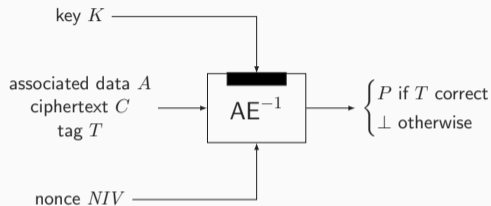
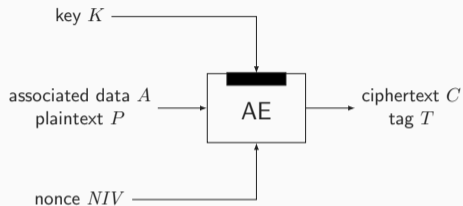
Authenticated Encryption



Role of Duplex

- Blockwise construction allows for processing different types of in-/output
- Usage of flag makes duplex-style encryption decryptable

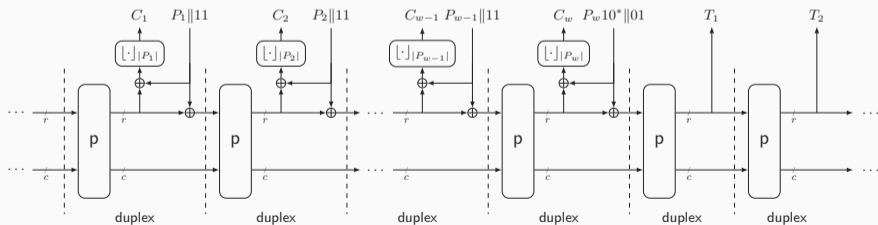
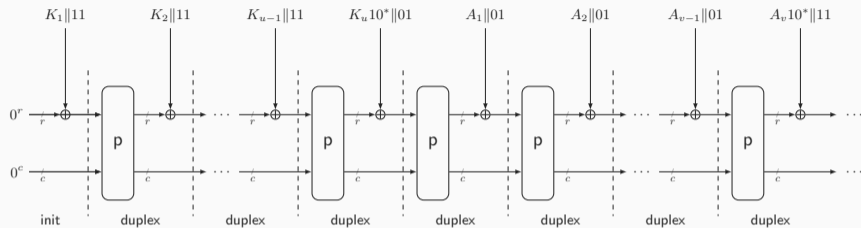
Authenticated Encryption



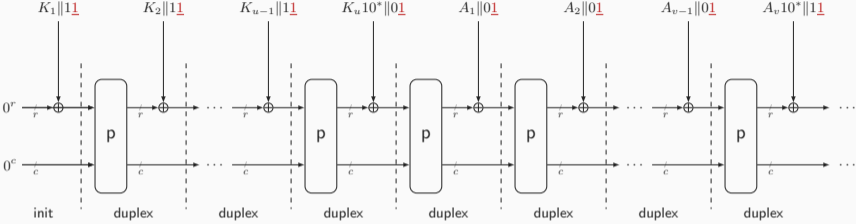
Role of Duplex

- Blockwise construction allows for processing different types of in-/output
- Usage of flag makes duplex-style encryption decryptable
(Although the flag is not a necessity for this)

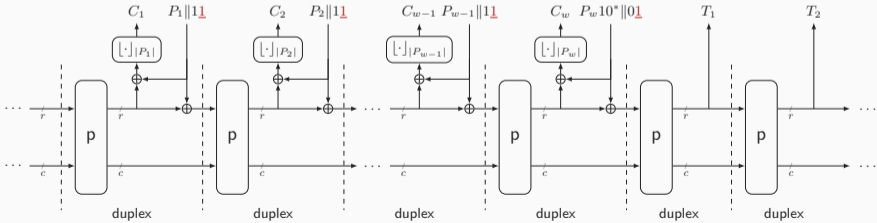
SpongeWrap [BDPV11a]



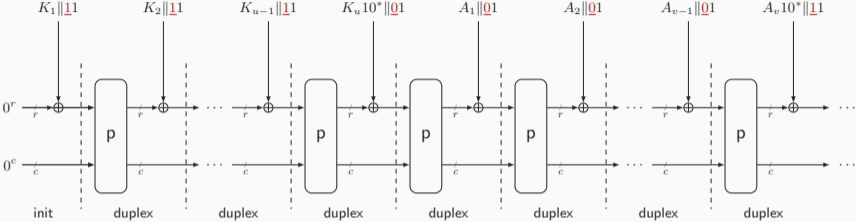
Issues with SpongeWrap



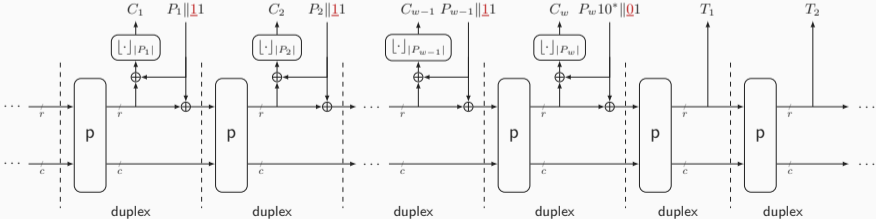
? always 1-padding



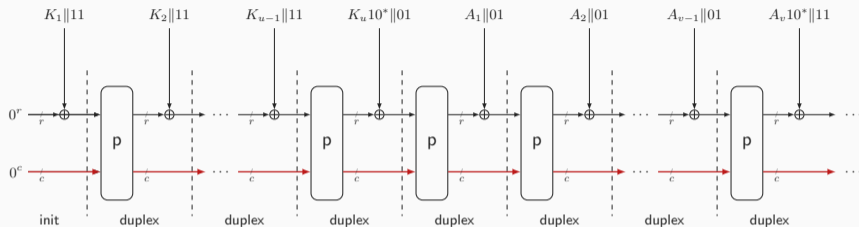
Issues with SpongeWrap



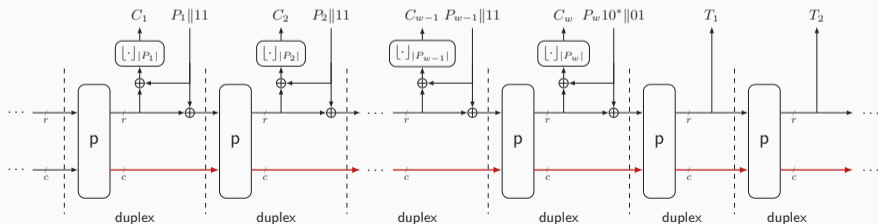
- ? always 1-padding
- ? off-phased domain separation



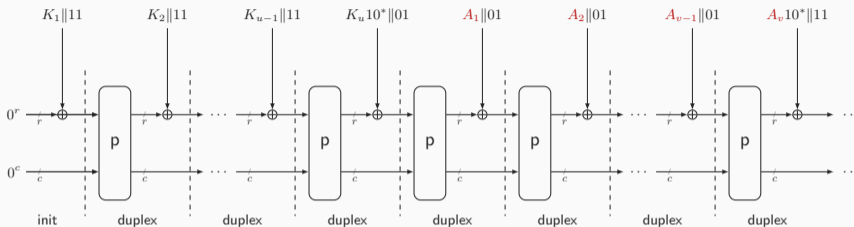
Issues with SpongeWrap



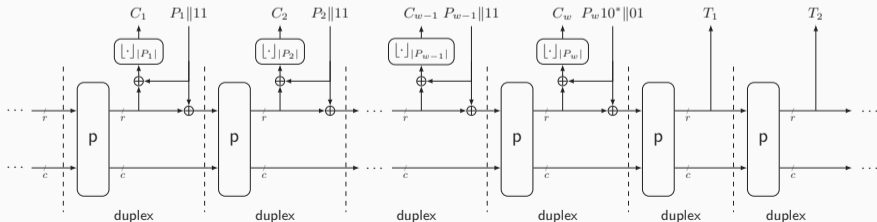
- ? always 1-padding
- ? off-phased domain separation
- ? no full-state absorption



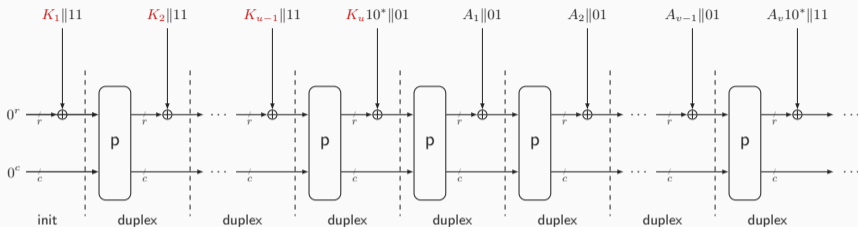
Issues with SpongeWrap



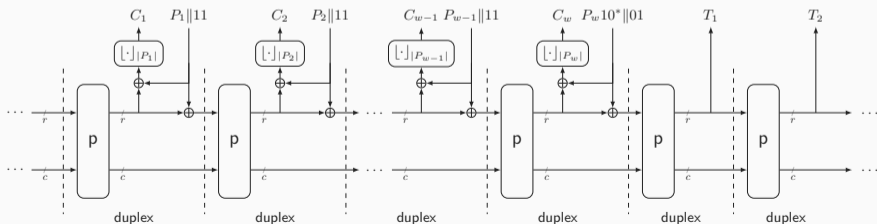
- ? always 1-padding
- ? off-phased domain separation
- ? no full-state absorption
- ? no explicit nonce



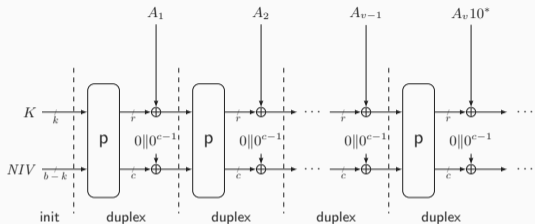
Issues with SpongeWrap



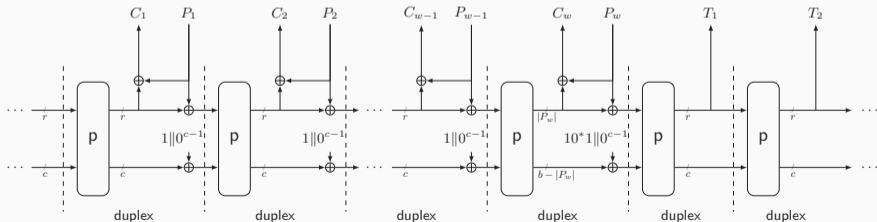
- ? always 1-padding
- ? off-phased domain separation
- ? no full-state absorption
- ? no explicit nonce
- ? blockwise key



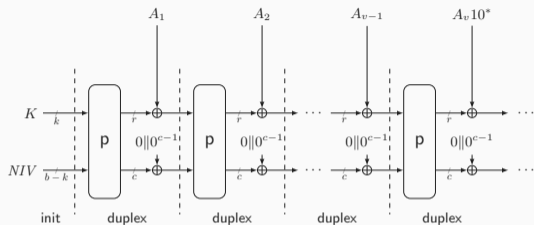
MonkeySpongeWrap: Encryption



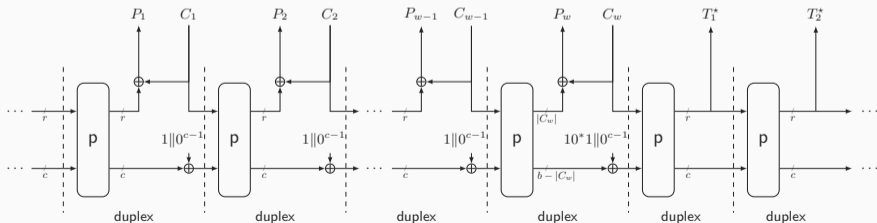
- State initialized using key and nonce
- Cleaned-up and synchronized domain separation
- Spill-over into inner part
- Used in Xoodyak and Gimli (a.o.)



MonkeySpongeWrap: Decryption



- Decryption similar to encryption
- Notable difference:
 - Processing of C
 - Duplexing with *flag = true*



MonkeySpongeWrap: Algorithm

Algorithm MonkeySpongeWrap[p]: ENC

Input: $(K, NIV, A, P) \in \{0, 1\}^k \times \{0, 1\}^{b-k} \times \{0, 1\}^* \times \{0, 1\}^*$

Output: $(C, T) \in \{0, 1\}^{|P|} \times \{0, 1\}^t$

Underlying keyed duplex: $\text{KD}[p]_{(K)}$

$(A_1, A_2, \dots, A_v) \leftarrow \text{pad}_r^{10^*}(A)$

$(P_1, P_2, \dots, P_w) \leftarrow \text{pad}_r^{10^*}(P)$

$C \leftarrow \emptyset$

$T \leftarrow \emptyset$

$\text{KD.init}(1, NIV)$

for $i = 1, \dots, v$ **do**

$\text{KD.duplex}(\text{false}, A_i \| 0 \| 0^{c-1})$ \triangleright discard output

for $i = 1, \dots, w$ **do**

$C \leftarrow C \parallel \text{KD.duplex}(\text{false}, P_i \| 1 \| 0^{c-1}) \oplus P_i$

for $i = 1, \dots, \lceil t/r \rceil$ **do**

$T \leftarrow T \parallel \text{KD.duplex}(\text{false}, 0^b)$

return $(\text{left}_{|P|}(C), \text{left}_t(T))$

Algorithm MonkeySpongeWrap[p]: DEC

Input: $(K, NIV, A, C, T) \in \{0, 1\}^k \times \{0, 1\}^{b-k} \times \{0, 1\}^* \times \{0, 1\}^* \times \{0, 1\}^t$

Output: $P \in \{0, 1\}^{|C|}$ or \perp

Underlying keyed duplex: $\text{KD}[p]_{(K)}$

$(A_1, A_2, \dots, A_v) \leftarrow \text{pad}_r^{10^*}(A)$

$(C_1, C_2, \dots, C_w) \leftarrow \text{pad}_r^{10^*}(C)$

$P \leftarrow \emptyset$

$T^* \leftarrow \emptyset$

$\text{KD.init}(1, NIV)$

for $i = 1, \dots, v$ **do**

$\text{KD.duplex}(\text{false}, A_i \| 0 \| 0^{c-1})$ \triangleright discard output

for $i = 1, \dots, w$ **do**

$P \leftarrow P \parallel \text{KD.duplex}(\text{true}, C_i \| 1 \| 0^{c-1}) \oplus C_i$

for $i = 1, \dots, \lceil t/r \rceil$ **do**

$T^* \leftarrow T^* \parallel \text{KD.duplex}(\text{false}, 0^b)$

return $\text{left}_t(T) = \text{left}_t(T^*) ? \text{left}_{|C|}(P) : \perp$

- Consider distinguisher D against AE security of MonkeySpongeWrap[p]

$$\mathbf{Adv}_{\text{MonkeySpongeWrap}}^{\text{ae}}(D) = \Delta_D(\text{ENC}[p]_K, \text{DEC}[p]_K, p^\pm ; R^{\text{ae}}, \perp, p^\pm)$$

- D can make: q_e encryption queries (total σ_e blocks),
 D can make: q_d decryption queries (total σ_d blocks),
 D can make: N primitive queries

MonkeySpongeWrap: Security (1)

- Consider distinguisher D against AE security of $\text{MonkeySpongeWrap}[p]$

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- Triangle inequality derivation slightly more involved than before:

$$\text{Adv}_{\text{MonkeySpongeWrap}}^{\text{ae}}(D) \leq \Delta_{D'}(\text{KD}[p]_K, p^\pm; \text{IXIF}[\text{ro}], p^\pm) + \frac{q_d}{2^t}$$

MonkeySpongeWrap: Security (1)

- Consider distinguisher D against AE security of MonkeySpongeWrap[p]

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- *What are the resources of D' ?*

MonkeySpongeWrap: Security (2)

- D can make: q_e encryption queries (total σ_e blocks),
D can make q_d decryption queries (total σ_d blocks),
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resources of D'	in terms of	resources of D
M : data complexity (calls to construction)		
N : time complexity (calls to primitive)	\longrightarrow	N
Q : number of init calls		
Q_{IV} : max # init calls for single IV		
L : # queries with repeated path		
Ω : # queries with overwriting outer part		

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<i>M</i> : data complexity (calls to construction)	→	$\sigma_e + \sigma_d$
<i>N</i> : time complexity (calls to primitive)	→	N
<i>Q</i> : number of init calls	→	$q_e + q_d$
Q_{IV} : max # init calls for single <i>IV</i>		
<i>L</i> : # queries with repeated path		
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MonkeySpongeWrap: Security (2)

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N : time complexity (calls to primitive)	→	N
Q : number of init calls	→	$q_e + q_d$
Q_{IV} : max # init calls for single IV	→	1
L : # queries with repeated path		
Ω : # queries with overwriting outer part		

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Ω : # queries with overwriting outer part	→	$\leq \sigma_d - 2q_d$

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From [DMV17] (in single-user setting):

$$\text{Adv}_{\text{KD}}(D') \leq \frac{2\nu_{r,c}^{2\sigma}(N+1)}{2^c} + \frac{\sigma_d N + \binom{\sigma_d}{2}}{2^c} + \frac{(\sigma-q)q}{2^{b-q}} + \frac{2\binom{\sigma}{2}}{2^b} + \frac{q(\sigma-q)}{2^{\min\{c+k,b\}}} + \frac{N}{2^k}$$

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attack of Gilbert et al. [GHKR23] “operates” here

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N : time complexity (calls to primitive)	→	N
Q : number of init calls	→	$q_e + q_d$
Q_{IV} : max # init calls for single IV	→	1
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attack of Gilbert et al. [GHKR23] “operates” here, with $\sigma_d, N \approx 2^{3c/4}$ 46 / 34